# Fuzzy Control 

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## Stick Balancing

Inverted pendulum



Balance an upright standing pole

Lower end of pole can be moved unrestrained along horizontal axis.

Mass $m$ at foot and mass $M$ at head.
Influence of mass of shaft itself is negligible.
Determine force $F$ (control variable) that is necessary to balance pole standing upright.

That is measurement of following output variables:

- angle $\theta$ of pole in relation to vertical axis,
- change of angle, i.e. triangular velocity $\dot{\theta}=\frac{d \theta}{d t}$

Both should converge to zero.

## Notation

Input variables $\xi_{1}, \ldots, \xi_{n}$, control variable $\eta$
Measurements: used to determine actual value of $\eta$

Assumption: $\xi_{i}, 1 \leq i \leq n$ is value of $X_{i}, \eta \in Y$
Solution: control function $\varphi$

$$
\begin{aligned}
\varphi: X_{1} \times \ldots \times X_{n} & \rightarrow Y \\
\left(x_{1}, \ldots, x_{n}\right) & \mapsto y
\end{aligned}
$$

## Example: Cartpole Problem (cont.)

Angle $\theta \in X_{1}=\left[-90^{\circ}, 90^{\circ}\right]$
Theoretically, every angle velocity $\dot{\theta}$ possible.
Extreme $\dot{\theta}$ are artificially achievable.
Assume $-45^{\circ} / \mathrm{s} \leq \dot{\theta} \leq 45^{\circ} / \mathrm{s}$ holds, i.e. $\dot{\theta} \in X_{2}=\left[-45^{\circ} / \mathrm{s}, 45^{\circ} / \mathrm{s}\right]$.

Absolute value of force $|F| \leq 10 \mathrm{~N}$.
Thus define $F \in Y=[-10 \mathrm{~N}, 10 \mathrm{~N}]$.

## Example: Cartpole Problem (cont.)

Differential equation of cartpole problem:
$(M+m) \sin ^{2} \theta \cdot l \cdot \ddot{\theta}+m \cdot l \cdot \sin \theta \cos \theta \cdot \dot{\theta}^{2}-(M+m) \cdot g \cdot \sin \theta=-F \cdot \cos \theta$
Compute $F(t)$ such that $\theta(t)$ and $\dot{\theta}(t)$ converge towards zero quickly.
Physical analysis demands knowledge about physical process.

In most real applications: No closed solution,
The standard is to use Runge Kutta Methods for systems of partial diffential equations for approximate solutions
New successful methods are often nature inspired, such as Model-based Fuzzy Control, Reinforcement Learning using data, evolutionary optimisation techniques

## Problems of Classical Approach

Often very difficult or even impossible to specify accurate mathematical model.

Description with differential equations is very complex.
Profound physical knowledge from engineer.
Exact solution can be very difficult.
Should be possible: to control process without physical-mathematical model. Human being knows how to balance a stick or to ride bike without knowing existence of differential equations.

Simulate behavior of human who knows how to control.
That is a knowledge-based analysis.
Directly ask expert to perform analysis.

Then expert specifies knowledge as linguistic rules, e.g. for cartpole problem:
"If $\theta$ is approximately zero and $\theta$ is also approximately zero, then $F$ has to be approximatelyzero,too."

The aim is to find a simple solution that is good enough.
With further steps (using data and learning methods) the solutions is refined, if necessary.

## Fuzzy Approach: Fuzzy Partitioning

1. Formulate set of linguistic rules:

Determine linguistic terms (represented by fuzzy sets).
$X_{1}, \ldots, X_{n}$ and $Y$ is partitioned into fuzzy sets.
Define $p_{1}$ distinct fuzzy sets $\mu_{1}^{(1)}, \ldots, \mu_{p_{1}}^{(1)} \in \mathcal{F}\left(X_{1}\right)$ on set $X_{1}$.
Associate linguistic term with each set.

## Coarse and Fine Fuzzy Partitions



## Fuzzy Approach: Fuzzy Partitioning II

$X_{1}$ corresponds to interval $[a, b]$ of real line, $\mu_{\rho_{1}}^{(1)} \in \mathcal{F}\left(X_{1}\right)$ are triangular functions

$$
\begin{aligned}
\mu_{x_{0}, \varepsilon}:[a, b] & \rightarrow[0,1] \\
x & \mapsto 1-\min \left\{\varepsilon \cdot\left|x-x_{0}\right|, 1\right\} .
\end{aligned}
$$

If $a<x_{1}<\ldots<x_{p_{1}}<b$, only $\mu_{2}^{(1)}, \ldots, \mu_{p_{1-1}}^{(1)}$ are triangular.
Boundaries are treated differently.

## Fuzzy Approach: Fuzzy Partitioning III

left fuzzy set:

$$
\begin{aligned}
& \mu_{1}^{(1)}:[a, b] \rightarrow[0,1] \\
& x \mapsto \begin{cases}1, & \text { if } x \leq x_{1} \\
1-\min \left\{\varepsilon \cdot\left(x-x_{1}\right), 1\right\} & \text { otherwise }\end{cases}
\end{aligned}
$$

right fuzzy set:

$$
\begin{array}{rlr}
\mu_{p_{1}}^{(1)}:[a, b] & \rightarrow[0,1] \\
x & \mapsto \begin{cases}1, & \text { if } x_{p_{1}} \leq x \\
1-\min \left\{\varepsilon \cdot\left(x_{p_{1}}-x\right), 1\right\} & \text { otherwise }\end{cases}
\end{array}
$$

## Example: Cartpole Problem (cont.)

$X_{1}$ partitioned into 7 fuzzy sets.

Similar fuzzy partitions for $X_{2}$ and $Y$.
Next step: specify rules
if $\xi_{1}$ is $A^{(1)}$ and $\ldots$ and $\xi_{n}$ is $A^{(n)}$ then $\eta$ is $B$,
$A^{(1)}, \ldots, A^{(n)}$ and $B$ represent linguistic terms corresponding to
$\mu^{(1)}, \ldots, \mu^{(n)}$ and $\mu$ according to $X_{1}, \ldots, X_{n}$ and $Y$.
Rule base consists of $k$ rules.

## Example: Cartpole Problem (cont.)



19 rules for cartpole problem, it is not necessary to determine all table entries. A table entry is interpreted as a rule: If $\theta$ is approximately zero and $\dot{\theta}$ is negative medium then $F$ is positivemedium.

## Mamdani Controller

## Architecture of a Mamdani Fuzzy Controller



## Qualitative Description of a Mamdani controller as a Rule System

|  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\dot{\vartheta}$ | nb | nm | ns | az | ps | pm | pb |
|  |  |  | ps | pb |  |  |  |
|  |  |  |  | pm |  |  |  |
|  |  |  |  |  |  |  |  |
|  | nm |  | ns | ps |  |  |  |
|  | nb | nm | ns | az | ps | pm | pb |
|  |  |  |  | ns | ps |  | pm |
|  |  |  |  | nm |  |  |  |
|  |  |  |  | nb | ns |  |  |
|  |  |  |  |  | ns |  |  |

19 rules for cartpole problem:
If $\vartheta$ is approximately zero and $\vartheta$ is negative medium then $F$ is positivemedium.

## Evaluation of a single rule



## Evaluation of a single rule



## Evaluation of several rules



## Definition of Table-based Control Function I

Given is the measurement $\left(x_{1}, \ldots, x_{n}\right) \in X_{1} \times \ldots \times X_{n}$
Consider a rule R

$$
\text { if } \mu^{(1)} \text { and } \ldots \text { and } \mu^{(n)} \text { then } \eta \text {. }
$$

The fuzzyfication unit computes for the input ( $\mathrm{x}_{1}, \ldots, x_{n}$ ) a , degree of fulfillment" of the premise of the rule:

For $1 \leq v \leq n$, the membership degree $\mu^{(v)}\left(x_{v}\right)$ is calculated. The n degrees are combined conjunctively with the min-operator and give the fulfillment degree $\alpha$

For each rule $R_{r}$ with $1 \leq r \leq k$, compute the fulfillment degree $\alpha_{r}$

## Definition of Table-based Control Function II

For the input ( $x_{1}, \ldots, x_{n}$ ) and a rule $R$ the decision unit calculates the output

$$
\begin{aligned}
\mu_{x_{1}, \ldots, x_{n}}^{\text {output }}: & Y \\
& \mapsto[0,1], \\
& \mapsto \min \left(\mu^{(1)}\left(x_{1}\right), \ldots, \mu^{(n)}\left(x_{n}\right), \eta(y)\right) .
\end{aligned}
$$

## Definition of Table-based Control Function III

The decision logic combines the output fuzzy sets from all rules $\mathrm{R}_{1}, \ldots, \mathrm{R}_{\mathrm{k}}$ by using the or-operator maximum. This results in the output fuzzy set

$$
\mu_{x_{1}, \ldots, x_{n}}^{\text {output }}: Y \rightarrow[0,1]
$$



Then $\mu_{x_{1}, \ldots, x_{n}}^{\text {output }}$ is passed to defuzzification interface.

## Definition of Table-based Control Function IV

Defuzzification interface derives crisp value from $\mu_{\chi_{1}, \ldots, x_{n}}^{\text {output }}$.

Most common defuzzification methods:

- max criterion,
- mean of maxima,
- center of gravity.


See Google Patents at defuzzification : More than 1080 methods

## Center of Gravity (COG) Method

Same preconditions as MOM method.
$\eta=$ center of gravity/area of $\mu_{x_{1}, \ldots, x_{n}}^{\text {output }}$
If $Y$ is finite, then

$$
\eta=\frac{\sum_{y_{i} \in Y} y_{i} \cdot \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}\left(y_{i}\right)}{\sum_{y_{i} \in Y} \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}\left(y_{i}\right)} .
$$

If $Y$ is infinite, then

$$
\eta=\frac{\int_{y \in Y} y \cdot \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}(y) d y}{\int_{y \in Y} \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}(y) d y} .
$$

## Example

Task: compute $\eta_{\text {COG }}$ and $\eta_{\text {MOM }}$ of fuzzy set shown below.


## Example for COG

## Continuous and Discrete Output Space

$$
\begin{aligned}
\eta_{\text {COG }} & =\frac{\int_{0}^{10} y \cdot \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}(y) d y}{\int_{0}^{10} \mu_{x_{1}, \ldots, x_{n}}^{\text {output }}(y) d y} \\
& =\frac{\int_{0}^{5} 0.4 y d y+\int_{5}^{7}(0.2 y-0.6) y d y+\int_{7}^{10} 0.8 y d y}{5 \cdot 0.4+2 \cdot \frac{0.8+0.4}{2}+3 \cdot 0.8} \\
& \approx \frac{38.7333}{5.6} \approx 6.917
\end{aligned}
$$

## Problem Cases for MOM and COG

Stone on the street, the car should not use COG (giving 0) but -1 or +1



Mamdani Control Applications

## Example: Engine Idle Speed Control

## VW 2000cc 116hp Motor (Golf GTI)



## M163B1 Fz SR stat.Zust. 20.8.92 MW(4500MP):827.13UpM



## Structure of the Fuzzy Controller

fuzzy controller


## Deviation of the Number of Revolutions dREV



## Gradient of the Number of Revolutions gREV



## Change of Current for Auxiliary Air Regulator dAARCUR



## Rule Base

If the deviation from the desired number of revolutions is negative small and the gradient is negative medium, then the change of the current for the auxiliary air regulation should be positive medium.
gREV

|  | nb | nm | ns | az | ps | pm | pb |
| ---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| nb | ph | pb | pb | pm | pm | ps | ps |
| nm | ph | pb | pm | pm | ps | ps | az |
| ns | pb | pm | ps | ps | az | az | az |
| dREV | az | ps | ps | az | az | az | nm |
| ns |  |  |  |  |  |  |  |
| ps | az | az | az | ns | ns | nm | nb |
| pm | az | ns | ns | ns | nb | nb | nh |
| pb | ns | ns | nm | nb | nb | nb | nh |

## Rule Base

If the deviation from the desired number of revolutions is negative small and the gradient is negative medium, then the change of the current for the auxiliary air regulation should be positive medium.
gREV

|  |  |  |  |  |  |  |  |  | nb | nm | ns | az | ps | pm | pb |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| nb | ph | pb | pb | pm | pm | ps | ps |  |  |  |  |  |  |  |  |
| nm | ph | pb | pm | pm | ps | ps | az |  |  |  |  |  |  |  |  |
| ns | pb | pm | ps | ps | az | az | az |  |  |  |  |  |  |  |  |
| dREV | ps | ps | az | az | az | nm | ns |  |  |  |  |  |  |  |  |
| ps | az | az | az | ns | ns | nm | nb |  |  |  |  |  |  |  |  |
| pm | az | ns | ns | ns | nb | nb | nh |  |  |  |  |  |  |  |  |
| pb | ns | ns | nm | nb | nb | nb | nh |  |  |  |  |  |  |  |  |



## Performance Characteristics




DRZO 10 - LFRSTRAUS - LFRSDRE

-DRZO_LO - LFRSTREI - LFRSDRZ

## Example: Automatic Gear Box AG4

Idea: car "watches" driver and classifies him/her into calm, normal, sportive (assign sport factor [0, 1]), or nervous (calm down driver).

Test car: different drivers, classification by expert (passenger).
Simultaneous measurement of 14 attributes, e.g. , speed, position of accelerator pedal, speed of accelerator pedal, kick down, steering wheel angle.

## Example: Automatic Gear Box

Continuously Adapting Gear Shift Schedule in VW New Beetle


## Example: Automatic Gear Box

## Technical Details

Optimized program on Digimat:
24 byte RAM
702 byte ROM
uses 7 Mamdani fuzzy rules


Runtime: 80 ms
12 times per second new sport factor is assigned.

In Series Line

Takagi Sugeno Control

## Takagi-Sugeno Controller

Proposed by Tomohiro Takagi and Michio Sugeno.
Modification/extension of Mamdani controller.
Both in common: fuzzy partitions of input domain $X_{1}, \ldots, X_{n}$.
Difference to Mamdani controller:

- no fuzzy partition of output domain $Y$, no defuzzification
- controller rules $R_{1}, \ldots, R_{k}$ are given by

$$
\begin{aligned}
& R_{r}: \text { if } \xi_{1} \text { is } A_{i_{1, r}}^{(1)} \text { and } \ldots \text { and } \xi_{n} \text { is } A_{i_{n, r}}^{(n)} \\
& \quad \text { then } \eta_{r}=f_{r}\left(\xi_{1}, \ldots, \xi_{n}\right),
\end{aligned}
$$

$f_{r}: X_{1} \times \ldots \times X_{n} \rightarrow Y$.

- Typically, $f_{r}$ is linear, i.e. $f_{r}\left(x_{1}, \ldots, x_{n}\right)=a_{0}^{(r)}+\sum_{i=1}^{n} a_{i}^{(r)} x_{i}$.


## Takagi-Sugeno Controller: Conclusion

For given input $\left(x_{1}, \ldots, x_{n}\right)$ and for each $R_{r}$, decision logic computes truth value $\alpha_{r}$ of each premise, and then $f_{r}\left(x_{1}, \ldots, x_{n}\right)$.

Analogously to Mamdani controller:

$$
\alpha_{r}=\min \left\{\mu_{i_{1, r}}^{(1)}\left(x_{1}\right), \ldots, \mu_{i_{n, r}}^{(n)}\left(x_{n}\right)\right\}
$$

Output equals crisp control value

$$
\eta=\frac{\sum_{r=1}^{k} \alpha_{r} \cdot f_{r}\left(x_{1}, \ldots, x_{n}\right)}{\sum_{r=1}^{k} \alpha_{r}}
$$

Thus no defuzzification method necessary.

## Example



If a certain clause " $x_{j}$ is $A_{i j, r}^{(j) "}$ in rule $R_{r}$ is missing, then $\mu_{i_{j, r}}\left(x_{j}\right) \equiv 1$ for all linguistic values $i_{j, r}$.
For instance, here $x_{2}$ in $R_{1}$, so $\mu_{i_{2,1}}\left(x_{2}\right) \equiv 1$ for all $i_{2,1}$.

## Example



If a certain clause " $x_{j}$ is $A_{i_{j, r}}^{(j) \text { " }}$ in rule $R_{r}$ is missing, then $\mu_{i_{j, r}}\left(x_{j}\right) \equiv 1$ for all linguistic values $i_{j, r}$.
For instance, here $x_{2}$ in $R_{1}$, so $\mu_{i, 1}\left(x_{2}\right) \equiv 1$ for all $i_{2,1}$.
input: $\quad\left(\xi_{1}, \xi_{2}\right)=(6,7)$

$$
\begin{array}{ll}
\alpha_{1}=1 / 2 \wedge 1=1 / 2 & \eta_{1}=6+7 / 2+1=10.5 \\
\alpha_{2}=1 / 2 \wedge 2 / 3=1 / 2 & \eta_{2}=-0.6+28+1.2=28.6 \\
\alpha_{3}=1 / 2 \wedge 1 / 3=1 / 3 & \eta_{3}=0.9 \cdot 6+0.7 \cdot 7+9=19.3 \\
\alpha_{4}=0 \wedge 1 / 3=0 & \eta_{4}=6+7 / 2+1=10.5
\end{array}
$$

output: $\quad \eta=f(6,7)=\frac{1 / 2 \cdot 10.5+1 / 2 \cdot 28.6+1 / 3 \cdot 19.3}{1 / 2+1 / 2+1 / 3}=19.5$


Pass a bend with a car at constant speed.
Measured inputs:
$\xi_{1}$ : distance of car to beginning of bend
$\xi_{2}$ : distance of car to inner barrier
$\xi_{3}$ : direction (angle) of car
$\xi_{4}$ : distance of car to outer barrier
$\eta=$ rotation speed of steering wheel
$X_{1}=[0 \mathrm{~cm}, 150 \mathrm{~cm}], X_{2}=[0 \mathrm{~cm}, 150 \mathrm{~cm}]$
$X_{3}=\left[-90^{\circ}, 90^{\circ}\right], X_{4}=[0 \mathrm{~cm}, 150 \mathrm{~cm}]$

## Fuzzy Partitions of $X_{1}$ and $X_{2}$



## Fuzzy Partitions of $X_{3}$ and $X_{4}$




## Rules for Car

$R_{r}$ : if $\xi_{1}$ is $A$ and $\xi_{2}$ is $B$ and $\xi_{3}$ is $C$ and $\xi_{4}$ is $D$

$$
\text { then } \begin{aligned}
\eta=p_{0}^{(A, B, C, D)} & +p_{1}^{(A, B, C, D)} \cdot \xi_{1}+p_{2}^{(A, B, C, D)} \cdot \xi_{2} \\
& +p_{3}^{(A, B, C, D)} \cdot \xi_{3}+p_{4}^{(A, B, C, D)} \cdot \xi_{4}
\end{aligned}
$$

$A \in\{$ small, medium, big $\}$
$B \in\{s m a l l, b i g\}$
$C \in\{$ outwards, forward, inwards $\}$
$D \in\{s m a l l\}$
$p_{0}^{(A, B, C, D)}, \ldots, p_{4}^{(A, B, C, D)} \in \mathbb{R}$

## Control Rules for the Car

| rule | $\xi_{1}$ | $\xi_{2}$ | $\xi_{3}$ | $\xi_{4}$ | $p_{0}$ | $p_{1}$ | $p_{2}$ | $p_{3}$ | -0.004 |
| :--- | :--- | :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: |
| $R_{1}$ | - | - | outwards | small | 3.000 | 0.000 | 0.000 | -0.045 | -0.090 |
| $R_{2}$ | - | - | forward | small | 3.000 | 0.000 | 0.000 | -0.030 | -0.000 |
| $R_{3}$ | small | small | outwards | - | 3.000 | -0.041 | 0.004 | 0.000 | 0.000 |
| $R_{4}$ | small | small | forward | - | 0.303 | -0.026 | 0.061 | -0.050 | 0.000 |
| $R_{5}$ | small | small | inwards | - | 0.000 | -0.025 | 0.070 | -0.075 | 0.000 |
| $R_{6}$ | small | big | outwards | - | 3.000 | -0.066 | 0.000 | -0.034 | 0.000 |
| $R_{7}$ | small | big | forward | - | 2.990 | -0.017 | 0.000 | -0.021 | 0.000 |
| $R_{8}$ | small | big | inwards | - | 1.500 | 0.025 | 0.000 | -0.050 | 0.000 |
| $R_{9}$ | medium | small | outwards | - | 3.000 | -0.017 | 0.005 | -0.036 | 0.000 |
| $R_{10}$ | medium | small | forward | - | 0.053 | -0.038 | 0.080 | -0.034 | 0.000 |
| $R_{11}$ | medium | small | inwards | - | -1.220 | -0.016 | 0.047 | -0.018 | 0.000 |
| $R_{12}$ | medium | big | outwards | - | 3.000 | -0.027 | 0.000 | -0.044 | 0.000 |
| $R_{13}$ | medium | big | forward | - | 7.000 | -0.049 | 0.000 | -0.041 | 0.000 |
| $R_{14}$ | medium | big | inwards | - | 4.000 | -0.025 | 0.000 | -0.100 | 0.000 |
| $R_{15}$ | big | small | outwards | - | 0.370 | 0.000 | 0.000 | -0.007 | 0.000 |
| $R_{16}$ | big | small | forward | - | -0.900 | 0.000 | 0.034 | -0.030 | 0.000 |
| $R_{17}$ | big | small | inwards | - | -1.500 | 0.000 | 0.005 | -0.100 | 0.000 |
| $R_{18}$ | big | big | outwards | - | 1.000 | 0.000 | 0.000 | -0.013 | 0.000 |
| $R_{19}$ | big | big | forward | - | 0.000 | 0.000 | 0.000 | -0.006 | 0.000 |
| $R_{20}$ | big | big | inwards | - | 0.000 | 0.000 | 0.000 | -0.010 | 0.000 |

## Sample Calculation

Assume that the car is 10 cm away from beginning of bend $\left(\xi_{1}=10\right)$.
The distance of the car to the inner barrier be $30 \mathrm{~cm}\left(\xi_{2}=30\right)$.
The distance of the car to the outer barrier be $50 \mathrm{~cm}\left(\xi_{4}=50\right)$.
The direction of the car be "forward" $\left(\xi_{3}=0\right)$.

Then according to all rules $R_{1}, \ldots, R_{20}$, only premises of $R_{4}$ and $R_{7}$ have a value $\neq 0$.

## Membership Degrees to Control Car

|  | small | medium | big |
| :---: | :---: | :---: | :---: |
| $\xi_{1}=10$ | 0.8 | 0 | 0 |
|  |  |  |  |
|  | small | big |  |
| $\xi_{2}=30$ | 0.25 | 0.167 |  |


|  | outwards | forward | inwards |
| :--- | :---: | :---: | :---: |
| $\xi_{3}=0$ | 0 | 1 | 0 |


|  | small |
| :---: | :---: |
| $\xi_{4}=50$ | 0 |

## Sample Calculation (cont.)

For the premise of $R_{4}$ and $R_{7}, \alpha_{4}=1 / 4$ and $\alpha_{7}=1 / 6$, resp.
The rules weights $\alpha_{4}=\frac{1 / 4}{1 / 4+1 / 6}=3 / 5$ for $R_{4}$ and $\alpha_{5}=2 / 5$ for $R_{7}$.
$R_{4}$ yields

$$
\begin{aligned}
\eta_{4} & =0.303-0.026 \cdot 10+0.061 \cdot 30-0.050 \cdot 0+0.000 \cdot 50 \\
& =1.873
\end{aligned}
$$

$R_{7}$ yields

$$
\begin{aligned}
\eta_{7} & =2.990-0.017 \cdot 10+0.000 \cdot 30-0.021 \cdot 0+0.000 \cdot 50 \\
& =2.820
\end{aligned}
$$

The final value for control variable is thus

$$
\eta=3 / 5 \cdot 1.873+2 / 5 \cdot 2.820=2.2518
$$

Fuzzy Control

Biggest success of fuzzy systems in industry and commerce.

Special kind of model-based non-linear control method.

Examples: technical systems

- Electrical engine moving an elevator,
- Heating installation

Goal: define certain behavior


- Engine should maintain certain number of revolutions per minute.
- Heating should guarantee certain room temperature.

